

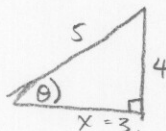
MATH 6 - QUIZ 6
16 MARCH 2012

Name: SOLUTIONS

NO CALCULATORS

1. Suppose $\sin \theta = \frac{4}{5}$ and θ is an acute angle (that is, $0 < \theta < \pi/2$). Find $\cos \theta$ and $\tan \theta$.

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$



$$x^2 + 4^2 = 5^2$$

$$x^2 = 25 - 16, \text{ so } x = 3.$$

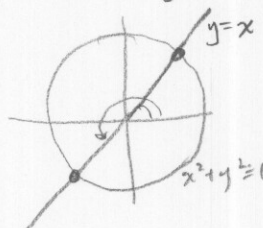
$$\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{3}{5}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{4}{3}$$

2. Suppose $\tan \theta = 1$. What are all possible values of θ between 0 and 2π ?

$$\text{If } \tan \theta = 1, \sin \theta = \cos \theta \text{ since } \tan \theta = \frac{\sin \theta}{\cos \theta}.$$

We can either realize that $\theta = \frac{\pi}{4}$ and $\theta = \frac{5\pi}{4}$ satisfy this, or use that $x=y$ and (x,y) are on the unit circle to draw:



and see that the angles we want are again

$$\boxed{\theta = \frac{\pi}{4} \text{ and } \theta = \frac{5\pi}{4}}$$