

MATH 42: MIDTERM 1

TOPICS COVERED

- Definitions (know them and be able to use them in simple proofs)
 - Divides, i.e. $a \mid b$
 - Congruence, i.e. $a \equiv b \pmod{c}$
 - Greatest common divisor, relatively prime
 - Unit
 - \mathbb{Z}_p and U_p
- Be able to compute
 - GCDs
 - solutions to linear diophantine equations ($ax + by = c$)
 - continued fractions and convergents
 - multiplicative inverses mod m
 - solutions (and number of solutions) to linear congruences $ax \equiv b \pmod{m}$
 - $\varphi(n)$
 - powers mod m
 - solutions to systems of two congruences (i.e. find x such that $x \equiv a \pmod{m}$ and $x \equiv b \pmod{n}$)
- Proofs
 - Proofs covered in class are fair game
 - Proofs from the homework are fair game
 - Induction
 - One-to-one and onto functions